

The Weekly Rigor

No. 166

“A mathematician is a machine for turning coffee into theorems.”

August 26, 2017

101 Problems in Calculating Derivatives Using the Chain Rule with Solutions (Part 2)

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|---|----------------------------------|---|
| 52. $f(x) = \ln(\arctan(x))$ | 53. $f(x) = \ln(\arcsin(x))$ | 54. $f(x) = (\ln(2x) + \ln(x))^3$ |
| 55. $f(x) = (\ln^2(x^5) - \ln(x))^{-2}$ | 56. $f(x) = \sin(3x)$ | 57. $f(x) = \cos\left(\frac{1}{2}x\right)$ |
| 58. $f(x) = \tan(3x)$ | 59. $f(x) = \sin(x^2)$ | 60. $f(x) = \cos\left(x^{\frac{3}{4}}\right)$ |
| 61. $f(x) = \tan(x^5)$ | 62. $f(x) = \sin^2(x)$ | 63. $f(x) = \cos^3(x)$ |
| 64. $f(x) = \tan^4(x)$ | 65. $f(x) = \sin^5(x^2)$ | 66. $f(x) = \cos^5(x^2)$ |
| 67. $f(x) = \tan^4(x^5)$ | 68. $f(x) = \sin(e^x)$ | 69. $f(x) = \tan(e^{3x})$ |
| 70. $f(x) = \arctan(3x)$ | 71. $f(x) = \arctan^2(x)$ | 72. $f(x) = \arctan^2(3x)$ |
| 73. $f(x) = \arcsin^3(x)$ | 74. $f(x) = \arcsin^3(x^2)$ | 75. $f(x) = \arccos(e^x)$ |
| 76. $f(x) = \sin(\arctan(x))$ | 77. $f(x) = \tan(\arcsin(x))$ | 78. $f(x) = \arctan(\sin(x))$ |
| 79. $f(x) = \arcsin(\tan(x))$ | 80. $f(x) = \arcsin(\arccos(x))$ | 81. $f(x) = \arctan(\arcsin(x))$ |
| 82. $f(x) = \ln(\sin(x))$ | 83. $f(x) = \ln(1 + \sqrt{x})$ | 84. $f(x) = \tan(\sin(x))$ |

$$\begin{array}{lll}
85. \ f(x) = (x^3 + 1)^3(5 + x^2)^4 & 86. \ f(x) = (x^2 + 3)^4(x^2 + 2)^{\frac{3}{2}} & 87. \ f(x) = (x^2 + x)^2(-x^2 + x^3)^{\frac{3}{2}} \\
88. \ f(x) = \sqrt{x^3 + 1}(x^2 + 1)^4 & 89. \ f(x) = \sin(2x)\cos(3x) & 90. \ f(x) = e^{2x}\tan^3(x) \\
91. \ f(x) = \frac{(x^2+3)^4}{(x^2+2)^{\frac{3}{2}}} & 92. \ f(x) = \frac{e^{2x}}{\sin(3x)} & 93. \ f(x) = \frac{\ln(4x)}{\arctan(3x)} \\
94. \ f(x) = e^{\cos(4x)} & 95. \ f(x) = e^{\tan(\ln(3x))} & 96. \ f(x) = \sin^3(\cos(2x)) \\
97. \ f(x) = \tan^4(\ln(e^{\sin(3x)})) & 98. \ f(x) = \ln^4(\cos(e^{\sin(x^2)})) & 99. \ f(x) = \arctan^4(\cos(\ln(5x))) \\
100. \ f(x) = \sin\left(\sin^2(\sin^3(x^4))\right) & 101. \ f(x) = \arctan(\sin(\ln(e^{\sqrt{x}}))) &
\end{array}$$

“Only he who never plays, never loses.”