

The Weekly Rigor

No. 179

“A mathematician is a machine for turning coffee into theorems.”

November 25, 2017

101 Problems in Calculating Derivatives Using the Chain Rule with Solutions (Part 15)

SET 4 PROBLEMS

Find the derivative $f'(x)$ of each of the following functions.

$$1. f(x) = \sin(e^x)$$

$$2. f(x) = e^{e^{2x}}$$

$$3. f(x) = \sqrt[3]{(x^2 + x)^2}$$

$$4. f(x) = e^{\arccos(2x)}$$

$$5. f(x) = \ln(3x^2)$$

$$6. f(x) = \sin^2(x)$$

$$7. f(x) = (x^3 + x^2 + 4)^{\frac{5}{3}}$$

$$8. f(x) = \ln(\arctan(x))$$

$$9. f(x) = \sqrt{x^3 + 1}(x^2 + 1)^4$$

$$10. f(x) = \arctan(\sin(\ln(e^{\sqrt{x}})))$$

$$11. f(x) = \frac{1}{\sqrt[3]{x-1}}$$

$$12. f(x) = \frac{e^{2x}}{\sin(3x)}$$

$$13. f(x) = \sqrt[5]{1 + x^{\frac{2}{3}}}$$

$$14. f(x) = \cos\left(x^{\frac{3}{4}}\right)$$

$$15. f(x) = (\ln^2(x^5) - \ln(x))^{-2}$$

$$16. f(x) = \arcsin(\arccos(x))$$

$$17. f(x) = \left(\frac{x^2-4}{x^3+7}\right)^5$$

$$18. f(x) = \sin^3(\cos(2x))$$

$$19. f(x) = \ln(x^2)$$

$$20. f(x) = \arctan(3x)$$

$$21. f(x) = e^{2x} \tan^3(x)$$

$$22. f(x) = e^{\frac{2}{5}x}$$

$$23. f(x) = \arcsin^3(x^2)$$

$$24. f(x) = \ln(3x)$$

$$25. f(x) = \sin\left(\sin^2(\sin^3(x^4))\right)$$

$$26. f(x) = (e^x + e^{-x})^3$$

$$27. f(x) = \tan^4(x)$$

$$28. f(x) = \ln(1 + \sqrt{x})$$

$$29. f(x) = \ln(e^{x^2})$$

$$30. f(x) = \sin(\arctan(x))$$

$$31. f(x) = \left(\frac{x^4 - x^5}{x^2 + x^3}\right)^3$$

$$32. f(x) = \ln^4(\cos(e^{\sin(x^2)}))$$

$$33. f(x) = \left(\frac{x^2 + 3}{x+1}\right)^3$$

$$34. f(x) = \sin(3x)$$

$$35. f(x) = \sqrt[4]{\sqrt{x} + x^{\frac{4}{3}}}$$

$$36. f(x) = \ln(\sin(x))$$

$$37. f(x) = e^{x^3}$$

$$38. f(x) = \cos^5(x^2)$$

$$39. f(x) = e^{e^x}$$

$$40. f(x) = \tan(3x)$$

$$41. f(x) = \frac{1}{(\sqrt[3]{x} + x^2)^{-2}}$$

$$42. f(x) = \arctan(\sin(x))$$

$$43. f(x) = (\sqrt{x^3 + 4})^3$$

$$44. f(x) = e^{\cos(4x)}$$

$$45. f(x) = (x^2 + x)^2(-x^2 + x^3)^{\frac{3}{2}}$$

$$46. f(x) = \frac{1}{\sqrt{(x^3 + x)^5}}$$

$$47. f(x) = \left(\frac{x-3}{x+8}\right)^4$$

$$48. f(x) = \tan(\sin(x))$$

$$49. f(x) = e^{\ln(x^2)}$$

$$50. f(x) = \arctan^2(3x)$$

$$51. f(x) = (x^2 + 3)^4$$

“Only he who never plays, never loses.”