## The Weekly Rigor

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"A mathematician is a machine for turning coffee into theorems."

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## 15 Problems in Solving Right Triangles (Part 3 of 4)

(Part 1)

## PROBLEMS

1. Given that  $x = 3\sin(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

2. Given that  $x = \sin(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

3. Given that  $x = \frac{1}{2}\sin(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

4. Given that  $x^2 = 3\sin^2(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

5. Given that  $x = a\sin(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

6. Given that  $x = 4 \tan(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

7. Given that  $x = \tan(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

8. Given that  $x = \sqrt{15} \tan(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

9. Given that  $2x = 3 \tan(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

10. Given that  $x = a \tan(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

11. Given that  $x = 5 \sec(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

12. Given that  $x = \sec(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

13. Given that  $5x = 2 \sec(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

14. Given that  $x^2 = 2 \sec(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

15. Given that  $x = a \sec(\theta)$ , find  $\sin(\theta)$ ,  $\cos(\theta)$ ,  $\tan(\theta)$ ,  $\sec(\theta)$ ,  $\csc(\theta)$ ,  $\cot(\theta)$  by constructing a right triangle consistent with the given information.

"Only he who never plays, never loses."

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