## The Weekly Rigor

No. 270

"A mathematician is a machine for turning coffee into theorems."

August 24, 2019

## **30 Problems Solving Simple Trigonometric Equations (Type II)** (Part 2)

## SELECTED SOLUTIONS

1.  $\csc(\theta) - 2 = 0 \implies \csc(\theta) = 2 \implies \frac{1}{\sin(\theta)} = 2 \implies \sin(\theta) = \frac{1}{2}.$ 

See WR no. 265, problem 1, for the rest of the solution.

13. 
$$\sec^2(\theta) - 4 = 0 \implies \sec^2(\theta) = 4 \implies \frac{1}{\cos^2(\theta)} = 4 \implies \cos^2(\theta) = \frac{1}{4}$$

See WR no. 267, problem 27, for the rest of the solution.

14.  $\sec(\theta) + 1 = 0 \implies \sec(\theta) = -1 \implies \frac{1}{\cos(\theta)} = -1 \implies \cos(\theta) = -1.$ 

See WR no. 266, problem 19, for the rest of the solution.

15. 
$$\csc(\theta) + \sqrt{2} = 0 \implies \csc(\theta) = -\sqrt{2} \implies \frac{1}{\sin(\theta)} = -\sqrt{2} \implies \sin(\theta) = \frac{-1}{\sqrt{2}}$$

See WR no. 265, problem 7, for the rest of the solution.

18. 
$$\sqrt{2} \operatorname{sec}(\theta) + 2 = 0 \implies \sqrt{2} \operatorname{sec}(\theta) = -2 \implies \operatorname{sec}(\theta) = \frac{-2}{\sqrt{2}} \implies$$
  
 $\implies \frac{1}{\cos(\theta)} = \frac{-2}{\sqrt{2}} \implies \cos(\theta) = \frac{-\sqrt{2}}{2} = \frac{-\sqrt{2}}{2} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{-2}{2\sqrt{2}} = \frac{-1}{\sqrt{2}}.$ 

See WR no. 266, problem 9, for the rest of the solution.

20. 
$$\csc(\theta) - 1 = 0 \implies \csc(\theta) = 1 \implies \frac{1}{\sin(\theta)} = 1 \implies \sin(\theta) = 1.$$

See WR no. 266, problem 13, for the rest of the solution.

22. 
$$3\sec^{2}(\theta) - 4 = 0 \implies 3\sec^{2}(\theta) = 4 \implies \sec^{2}(\theta) = \frac{4}{3} \implies$$
  

$$\Rightarrow \frac{1}{\cos^{2}(\theta)} = \frac{4}{3} \implies \cos^{2}(\theta) = \frac{3}{4}.$$

See WR no. 267, problem 25, for the rest of the solution.

"Only he who never plays, never loses."

Written and published every Saturday by Richard Shedenhelm