

# The Weekly Rigor

No. 286

“A mathematician is a machine for turning coffee into theorems.”

December 14, 2019

## 60 Problems in Factoring by a Mixture of Methods (Part 3)

### ANSWERS

|  |  |
|--|--|
| 1. $(x + 5y)(x^2 - 5xy + 25y^2)$                 | 2. $4xy^2(2x^4 + 3y)$                      |
| 3. $(2 - x - y)(x^2 + y^2 + 2x + 2y + 2xy + 4)$  | 4. Prime                                   |
| 5. $(2x + 3)(x + 6)$                             | 6. $4(3t^3 - 2t^2 - 6t + 5)$               |
| 7. $m(m^2 + 1)$                                  | 8. $(3y - 2)(y^2 - 2)$                     |
| 9. $(x^2 + y^2)(x^4 - x^2y^2 + y^4)$             | 10. $(\theta + 5)(\theta - 5)$             |
| 11. $(x + 3)(x + 2)(x - 2)$                      | 12. $(\alpha + 7)(\alpha + 3)$             |
| 13. $(x + 4)(x^2 - 4x + 16)$                     | 14. Prime                                  |
| 15. $3(x + 5)(x - 5)$                            | 16. $(11m + n)(11m - n)$                   |
| 17. $27(x - 3)(x^2 - 3x + 3)$                    | 18. $(2\alpha + 3\beta)(2\alpha - 3\beta)$ |
| 19. $4x(3x + 2)(x - 1)$                          | 20. $(x + 2)(x - 2)(5x + 3)$               |
| 21. $-2(3x^2 + 24x + 49)$                        | 22. $(5t + 3)(t + 4)$                      |
| 23. $(x + y + 2)(x^2 + y^2 - 2x - 2y + 2xy + 4)$ | 24. $12x^3(x - 1)(x^2 + 2)$                |
| 25. $(4x - 3y)(16x^2 + 12xy + 9y^2)$             | 26. $x^2(x + 1)$                           |
| 27. $2(5m + 3n^2)(n + 5)$                        | 28. $(x + 2)(x - 2)(x^4 + 4x^2 + 16)$      |
| 29. $(4x + y)(16x^2 - 4xy + y^2)$                | 30. $x(x + 1)(x - 1)$                      |

|  |  |
|--|--|
| 31. $(7x + 1)(y + 2x^2)(y - 2x^2)$                     | 32. $10x(2x - 1)(x + 3)$                     |
| 33. $(3 + 2x)(9 - 6x + 4x^2)$                          | 34. $2r(4r^2 + 5)(3r + 5)$                   |
| 35. $(3x - 1)(9x^2 + 3x + 1)$                          | 36. $(x^2 + 1)(x + 1)(x - 1)(3x + 5)$        |
| 37. $(3x + 2y)(x + y)$                                 | 38. $(e^x + 1)(e^x - 1)$                     |
| 39. $(4 + x)(16 - 4x + x^2)$                           | 40. $(1 + \cos(\theta))(1 - \cos(\theta))$   |
| 41. $(e^x - \ln(x))(e^{2x} + e^x \ln(x) + \ln^2(x))$   | 42. $(e^x - 2)(e^{2x} + 5)$                  |
| 43. $(2 - x)(4 + 2x + x^2)$                            | 44. $(3e^x - 5)(e^x + 1)$                    |
| 45. $(x + 3)(x^2 - 3x + 9)$                            | 46. $(e^{2x} + 4)(e^x + 2)(e^x - 2)$         |
| 47. $3e^x(2e^x - 1)(3e^x - 4)$                         | 48. $(xy + 3)(xy - 3)$                       |
| 49. $(3x - 1)^2$                                       | 50. $(\ln(x) + 3)(\ln(x) - 3)$               |
| 51. $(\ln(x) + 2)(\ln^2(x) - 2\ln(x) + 4)$             | 52. $(\sin(x) + \cos(x))(\sin(x) - \cos(x))$ |
| 53. $(\sin(\theta) + 1)(\sin(\theta) - 1)$             | 54. $(\ln(x) - 3)(\ln^2(x) + 3\ln(x) + 9)$   |
| 55. $(e^x + 4)(e^x - 4)$                               | 56. $(e^x - 2)(e^{2x} + 2e^x + 4)$           |
| 57. $e^{2x}(e^x + 1)(e^x - 1)$                         | 58. $(e^x + 1)(e^{2x} - e^x + 1)$            |
| 59. $[e^x \sin(x) + x \ln(x)][e^x \sin(x) - x \ln(x)]$ | 60. $(x - 4y)(2x - y)$                       |

“Only he who never plays, never loses.”